Homework 7 Due Tuesday 5/3/2011 in discussion section

Name:

Section Number:

This cover sheet must be attached as the top page of your homework.

- 1. A ball is thrown directly upward from ground level with an initial velocity v(0) = 96 ft/s. Assuming that the ball's only acceleration is that due to gravity (i.e., $a(t) = -32 ft/s^2$), determine the maximum height reached by the ball and the time it takes to return to ground level.
- 2. Given the following integral:

$$\int_{1}^{3} 4x^2 + 2 \, dx$$

- (a) Estimate the value of the integral using a Riemann sum $S_n = \sum_{k=1}^n f(a+k\Delta x)\Delta x$ with n = 4 and using right endpoints.
- (b) Evaluate the definite integral **using the definition**. Use equal width subintervals and evaluate the function at right endpoints. So in this case, you are evaluating

$$\lim_{n \to \infty} \sum_{k=1}^{n} f(a + k\Delta x) \Delta x,$$

where $\Delta x = \frac{b-a}{n}$.

- 3. Find the area of the region under the curve given by $y = t\sqrt{t^2 + 9}$ on [0, 4].
- 4. Find the average value of the function $f(x) = \frac{x}{\sqrt{x^2+1}}$ on the interval [0,3].