

Hardy & Wright: *An Introduction to Number Theory*

Section XXIII: Kronecker's Theorems

Theorem 438. If  $\mathbf{q}$  is irrational,  $\mathbf{a}$  is arbitrary, and  $N$  and  $\mathbf{e}$  are positive, then there are integers  $n$  and  $p$  such that  $n > N$  and

$$(23.1.2) \quad |n\mathbf{q} - p - \mathbf{a}| < \mathbf{e}$$

Theorem 439. If  $\mathbf{q}$  is irrational, then the set of points  $(n \mathbf{q}) = n \mathbf{q} - [n \mathbf{q}]$  is dense in the interval  $(0,1)$ .