## Math 4363 - Combinatorics Homework 2

## Due in Class - Thursday 6 February 2020

- 1. A committee of five people is chosen from a group of 10 men and 12 women.
  - (a) How many ways can the committee be formed if it is to contain at least two women?
  - (b) How many ways can the committee be formed if, in addition, one particular man and one particular woman refuse to serve on the committee together?
- **2.** How many sets of three integers between 1 and 20 are possible if no two consecutive integers are to be in a set?
- **3.** There are 100 students at a school and three dormitories A, B and C, with capacities 25, 35 and 40 respectively.
  - (a) How many ways are there to fill the dormitories?
  - (b) How many ways are there to fill the dormitories if 50 students are men and 50 students are women; and dormitory A is all male, dormitory B is all female and dormitory C is co-ed.
- **4.** How many ways can two red rooks and four blue rooks be placed on a 8 by 8 board so that no two rooks can attack one another?
- 5. Determine the number of *r*-permutations of the multiset

 $\{1 \cdot a_1, \infty \cdot a_2, \infty \cdot a_3, \cdots, \infty \cdot a_k\}?$