

# THE FROBENIUS FUNCTOR AND RINGS OF PRIME CHARACTERISTIC

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ABSTRACT. Let  $A$  be an  $m$  by  $n$  matrix with entries from a field of prime characteristic  $p$ . What happens to the kernel of  $A$  when we raise each entry to the  $p$ th power? We will answer this question and consider its generalization to matrices with entries from a commutative ring of prime characteristic  $p$ . Prime characteristic rings have played an important role in many recent advances in commutative algebra, and we will explore some classical and recent results in the study of such rings.