

## MATH 3360 HOMEWORK ASSIGNMENT 18

DUE ON TUESDAY 5 MAY 2020

- (1) Let  $f(x) = x^4 + 5x^2 + 3$ .
  - (a) Determine a prime  $p$  such that  $f(2) = 0$  over the field  $\mathbb{Z}_p$ .
  - (b) Factor  $f(x)$  as  $(x - 2)q(x)$  in  $\mathbb{Z}_p[x]$ .
  
- (2) Use the Euclidian algorithm to find the greatest common divisor in  $\mathbb{Z}_5[x]$  of  $f(x) = x^3 - 2x + 1$  and  $g(x) = x^2 - x - 2$ .