## Mid Term Exam 3

- Answer all questions
- Show all steps in your calculations
- No calculators or computers allowed

1. Solve the following linear differential equation using an integrating factor

$$
\frac{d y}{d x}+\frac{1}{x} y=\frac{1}{x}
$$

2. Solve the following differential equation using separation of variables:

You need to separate the variables and do partial fractions

$$
x y d x=(x-4)(x-5) d y
$$

3. Calculate the following improper integrals or argue that they do not exist:

Note that the functions are discontinuous so that you need to split the integrals
i. $\int_{0}^{3} \frac{1}{(x-1)^{5 / 6}} d x$
ii. $\int_{-1}^{1} \frac{1}{x} d x$
4. Calculate the sum of the first $n$ terms of the following sequences
i. $2,4,6,8,10, \ldots$
ii. $1, \frac{1}{3}, \frac{1}{9}, \frac{1}{27}, \frac{1}{81}, \ldots$
5. Using the integral test, determine if the following series converges or diverges.

$$
\sum_{k=1}^{\infty} k e^{-k^{2}}
$$

