

MATH 1351 TI-85 EXERCISE IV
Graphical investigations of limiting behavior

Name: _____ SID: _____

1. Graph each of the following in the **ZDECM** viewing window. Explain the presence of the discontinuity at $x = 1$ and discuss the limiting behavior as x approaches 1.

a. $y = (x^2 - 1) / (x - 1)$

b. $y = |x^2 - 1| / (x - 1)$

c. $y = (x^2 - 1) / |x - 1|$

2. In problem #1 write each function in terms of equations of lines on various intervals. (Problems 41 - 43 on page 20 are examples of such.)

a

y = _____

b..

y = _____

c.

y = _____

3. a. Estimate the limit to 5 decimal places as x goes to 0 of the expression $(1 + x)^{1/x}$.

b. Compute e^1 .

4. Graph the function $y = (\sin x) / x$ in **RADIAN MODE**. Using **TRACE** and **ZOOM** estimate the limit as x approaches 0. _____

5. a. Repeat exercise #4 in **DEGREE MODE**. The limit to 5 decimal places is approximately _____

b. Recall that 1 degree equals $\text{Pi}/180$ radian . Compute $\text{Pi}/180$. _____

6. Return to **RADIAN MODE**, sketch the graph and “evaluate” the limiting behavior as x approaches 0 for each of the following functions.

a. $y = \sin (1 / x)$

b. $y = x \sin (1 / x)$

c. $y = x^2 \sin (1 / x)$

In your own words describe the difference you observe between the graphs of a, b and c. (It might help to “overlay” the graphs of $y = 1$ & $y = -1$ on the graph of a, the graphs of $y = x$ & $y = -x$ on the graph of b, and the graphs of $y = x^2$ and $y = -x^2$ on the graph of c.)