

## MATH 1351 TI-85 EXERCISE II

### Part 1

#### Introduction to graphing

Name: \_\_\_\_\_ SID: \_\_\_\_\_

To activate the TI-85 graphing utility choose **GRAPH** from the keyboard. A screen menu will appear. The little wedge at the right indicates there is more stuff in the menu. To see it press **MORE** from the keyboard. Do this until you cycle through the entire GRAPH menu. There are 13 items in this menu, of which we will use 8 during the course of these exercises.

Any screen menu item is accessed via pressing the **F** key directly beneath it. Choose **y(x)=** from the graph screen menu. (Press **F1** from the keyboard.) This activates a new screen menu (again with more stuff in it). Pressing **EXIT** from the keyboard will exit this menu and activate the previous menu. Try it and then return to the **y(x)=** menu.

For our purpose it is best to begin with a “clean slate.” If there are functions defined on your screen ( $y1 = \text{something}$ ,  $y2 = \text{something}$ , etc) choose **DELf** (short for delete f) from the screen menu successively until they are all deleted. Now the blinking cursor is asking you to define the function  $y1$ . Define

$$y1 = x.$$

To do this either choose **x-var** (x as a variable) from the keyboard or choose **x** from the screen menu. Either of these tells the TI-85 that x represents a variable, not just the letter “x”. Choose **EXIT** from the keyboard to return to the GRAPH menu, and then choose **GRAPH** from the screen menu to graph the function  $y1 = x$ . To get the viewing window we want for this exercise, choose **ZOOM** from the GRAPH menu and then **ZSTD** (zoom standard) from the ZOOM menu.

Return to the **y(x)=** menu. Press the *arrow down* button. The TI-85 is now asking you to define a new function  $y2$ . Define

$$y2 = y1^2.$$

To do this choose the variable **y** from the screen menu, then **1**, and either **x squared** or **^2** from the keyboard. What is the function  $y2$  in terms of x?

$$y2 = \text{_____} \text{ in terms of } x.$$

Now choose **GRAPH** from the GRAPH menu. You should observe that both  $y1$  and  $y2$  are graphed on the same axes.

Question: Does the graph of  $y2$  dip below the graph of  $y1$  near  $(0, 0)$ ?

To answer this question we need to zoom in on  $(0, 0)$  to get a closer view of the two graphs. Choose **ZOOM** then **ZIN** from the appropriate screen menus. Notice that the x and y coordinates of the cursor position are displayed at the bottom of your screen, the default position being at the center of the screen. The *up/down/left/right* arrows could be used to position the cursor anywhere on the screen; however, we will leave it at  $(0,0)$  since that is the point we want

to observe more closely. Choose **ENTER** to activate the zoom. One zoom in is enough to answer the question. In fact we observe that  $y_2$  does dip below  $y_1$ . In what interval does this occur? \_\_\_\_\_ Explain this phenomenon in terms of the relation between numbers and their squares. \_\_\_\_\_

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Now define a new function

$$y_3 = y_2 + y_1.$$

What is this function in terms of  $x$ ?

$$y_3 = \text{_____} \text{ in terms of } x.$$

Graph  $y_1$  and  $y_3$  on the same axes with the standard viewing window. Note, to graph only  $y_1$  and  $y_3$  you need to “turn off”  $y_2$ . The item **SELECT** (short for select) in the  $y(x)=$  screen menu acts as an on/off switch. Arrow up or down until the cursor is blinking on  $y_2$ , then choose **SELECT** from the screen menu to “turn off”  $y_2$ . You can tell whether a function is “on” or “off” by whether or not the = is highlighted. The same procedure would turn an “off” function “on.”

With  $y_1$  and  $y_3$  graphed on the same axes we ask the same question as above.

Question: Does the graph of  $y_3$  dip below the graph of  $y_1$  near  $(0,0)$ ?

We approach the question in the same way. Zoom in on  $(0,0)$  and see what happens. This time 1 zoom is maybe not enough. To zoom in again simply press **ENTER** again. What happens? \_\_\_\_\_

What happens after the third zoom in? \_\_\_\_\_

Can this question be answered by looking only at the graphs on the TI-85? \_\_\_\_\_  
Explain. \_\_\_\_\_

Describe what appears to be happening as we zoom in on the graphs of  $y_1$  and  $y_2$  closer and closer to  $(0,0)$ . \_\_\_\_\_

Attach a sketch the graph of the function

$$y = (x^2)(x+1)(x-1)^3.$$

(Pressing **CLEAR** after graphing removes the screen menu from the screen, thus producing a nicer picture. To get the menu back press **EXIT**)

Just for fun, graph some other polynomial functions (not just quadratics), choose a point on the graph and zoom in 3 or 4 times on that point. Each time the graph should eventually start to look like a line. Maybe we ought to really understand lines before worrying about more complicated functional behavior.

Part 2

**Lines, lines, and more lines**

Delete the functions in your graphing utility and began anew with the following set. Graph the function  $y_1 = (1/3)x$ . Try the **ZDECM** viewing window from the **ZOOM** menu. Next graph (on the same axes)  $y_2 = (3/4)x$ , then  $y_3 = x$ , then  $y_4 = 2x$ , and  $y_5 = 3x$ . What is the effect on the graph of choosing a bigger value for  $b$  ( $>0$ ) in the function  $y = bx$ ? \_\_\_\_\_

Repeat the above exercise with the value of each coefficient of  $x$  negated. For example, let  $y_1 = (-1/3)x$ , and so on. (Negation is not the same operation as subtraction. After all, subtraction is a binary operation: to subtract one number from another you have to have two numbers to start with. To negate a number choose (-) from the keyboard.) What is the effect on the graph of choosing a bigger value for  $b$  ( $b > 0$ ) in the function  $y = -bx$ ? \_\_\_\_\_

The question of just what is meant by “steepness of a line” arises. To consider this question graph the line  $y_1 = 2x$ . Use the **ZDECM** followed by the **ZSQR** viewing window. (ZSQR is short for zoom square, and has the effect of making the  $x$  and  $y$  axes have the same scale. Since the screen is not a square, the default  $x$  and  $y$  scales are different.) Exit back to the **GRAPH** menu and choose **TRACE**. The cursor appears at the center of the graph, *arrow left* causes the cursor to trace the graph to the left, *arrow right* causes it to trace the graph to the right. In addition the  $x$  and  $y$  coordinates of the cursor are displayed at the bottom of the screen. As you trace along the graph of  $y_1 = 2x$  to the right, what is the change in the value of  $x$  from one point to the next? \_\_\_\_\_ (It might interest you to know that ZDECM is short for “zoom decimal.”) What is the corresponding change in the value of  $y$  from one point to the next? \_\_\_\_\_ We define

*the slope of a line to be (the change in  $y$ ) / (the change in  $x$ ).*

This is our measure of the steepness of a line. Use **TRACE** to determine the slope of each of the above lines, and record the results in the spaces provided.

$y = (1/3)x$ :	slope = _____	$y = (3/4)x$ :	slope = _____
$y = x$ :	slope = _____	$y = 2x$ :	slope = _____
$y = 3x$ :	slope = _____	$y = (-1/3)x$ :	slope = _____
$y = -2x$ :	slope = _____	$y = -3x$ :	slope = _____
$y = mx$ :	slope = _____	$y = 3$ :	slope = _____

Graph the lines given by  $y = 2x + b$  for various values of  $b$ . What is the effect of changing the values of  $b$  on these graphs, and what is the relation between all these graphs? \_\_\_\_\_