

# Final Exam Practice

1. Let  $(X, Y)$  admits the following joint density

$$f(x, y) = 2e^{-x-y}, \quad x > y > 0.$$

- (1) Find  $P(X \leq 2Y)$ .
- (2) Find  $Ee^Y$ .
- (3) Find  $f_{X|Y}(x|y)$ .
- (4) Find  $E[X|Y = 2]$ .

2. Define the Binomial, Geometric, Poisson, Negative Binomial and Hypergeometric distributions.

3. Let  $X$  admit the density function

$$f(x) = e^{-x}, \quad x \geq 0$$

- (1) Find the density of  $U = 3X + 2$ .
- (2) Find the density of  $U = X^2$ .

4. Let  $X_1, \dots, X_n$  be independent random variables with same density

$$f(x) = e^{-x}, \quad x > 0.$$

Find the distribution of  $X_{(1)}$  and  $X_{(n)}$ .

5. Let  $X$  have the density

$$f(x) = 2e^{-2x}, \quad x > 0.$$

Find  $P(X > 2)$  and  $EX$ .

6. It is known that a quarter of the population in Lubbock catches a specific flu. An investigation shows that in a test, the probability for correct positive and correct negative are 0.81 and 0.99. Denis receives 1 positive result and 1 negative result. What is the probability that Denis catches the flu?

7. The random variable  $X$  admits the following distribution

$x$	-1	0	1
$P(X = x)$	0.1	0.5	$p$

- (1) Find  $p$ .
- (2) Find the mean and variance of  $X$ .