

Answer the problems on **separate** paper. You do not need to rewrite the problem statements on your answer sheets. Do your own work. Show **all relevant steps** which lead to your solutions. Attach this question sheet to the front of your answer sheets.

1. (8 pts) Let  $f(x, y) = (x + y^2)e^{x-4y}$ . Find  $\frac{\partial f}{\partial x}$  and  $\frac{df}{dy}$ .
2. (25 pts) Let  $f(x, y) = (x^2 - y)\cos(xy)$ . Find  $\frac{\partial f}{\partial x}$ ,  $\frac{df}{dy}$ ,  $\frac{\partial^2 f}{\partial x^2}$ ,  $\frac{\partial^2 f}{\partial y^2}$  and  $\frac{\partial^2 f}{\partial y \partial x}$ .
3. (12 pts) The formula for impedance in a circuit is  $Z = \sqrt{4X^2 + R^2}$ . If  $X$  is measured to be  $20.00\ \Omega$  with an error of  $\pm 0.04\ \Omega$  and  $R$  is measured to be  $30.00\ \Omega$  with an error of  $\pm 0.05\ \Omega$ , (use the total differential to) find the approximate maximum error in  $Z$ .
4. (20 pts) Find and classify any possible maxima and/or minima of the function  $f(x, y) = x^2 - y^3 + 3x + 12y + 4$ .
5. (12 pts) Evaluate the iterated integral  $\int_0^2 \int_0^y (4y + 4x) dx dy$ .
6. Omit
7. (12 pts) Use an iterated integral to find the area of the region  $R$  where  $R$  is the region in the first quadrant bounded by the curves  $y = \sqrt{x}$ ,  $x = 2$  and the  $x$ -axis.
8. (12 pts) Find the volume of the solid in the first octant which lies above the triangular region bounded by the planes  $x = 0$ ,  $y = 0$ , and  $x + y = 2$  and below the paraboloid  $z = 4 - x^2 - y^2$ .