Math 4350.004 Spring 2018 In-Class Problems # 3

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1. The power set of the natural numbers $\mathcal{P}(\mathbb{N})$ is uncountable, (Cantor's Theorem, p. 21). Other sets that are uncountable include: \mathbb{R} , the irrationals, finite or infinite intervals. Name 2 other sets, different from the ones already named, that are uncountable.

2. Write out the first 5 terms of the following sequences.

(a)
$$x_n := \frac{(-1)^n}{n(n+1)}$$

(b)
$$x_1 := 2$$
, $x_{n+1} := \frac{1}{2}(x_n + 2/x_n)$

3. Use the definition of the limit of a sequence to prove the following limit: $\lim \left(\frac{(-1)^n}{n(n+1)}\right) = 0$.