Abstract. Representation theory of finite groups deals with the realization of finite groups as matrix groups. After a summary of the basic theory we will have a look at the fundamental questions in representation theory and how these questions are studied from the computational point of view.