

1/28/2014

9.7

2D

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

\* a circular paraboloid is a special case of an Elliptical Paraboloid

$$(y-k) = \frac{(x-h)^2}{a^2}$$

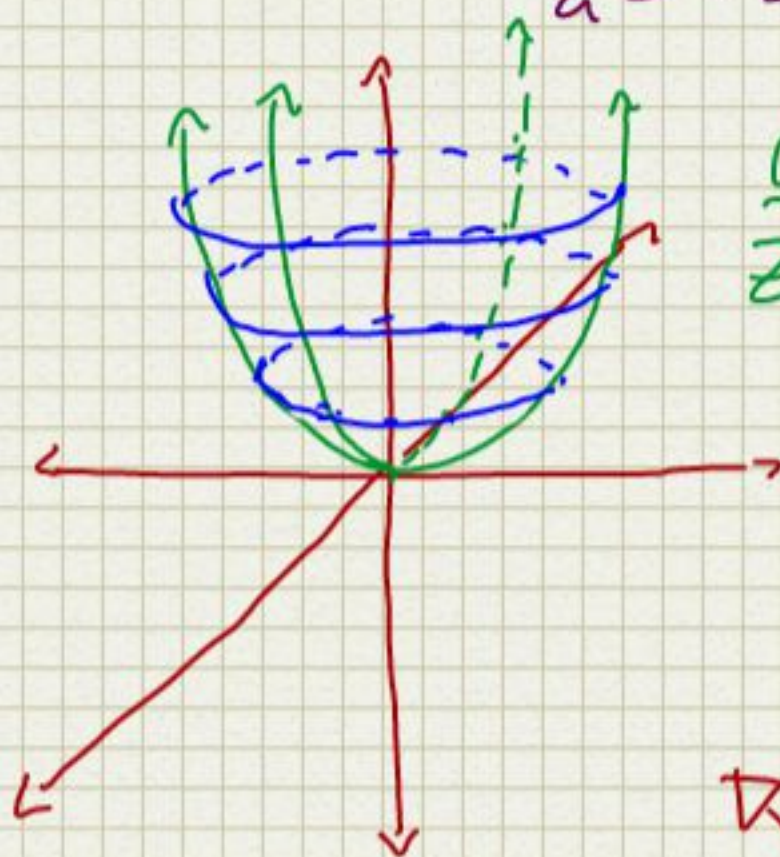
$$x = \frac{y^2}{2} + \frac{z^2}{4}$$

vertex at (0,0)

\* Elliptic Paraboloid that opens towards x-axis

3D Ellipsoid

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} + \frac{(z-l)^2}{c^2} = 1$$



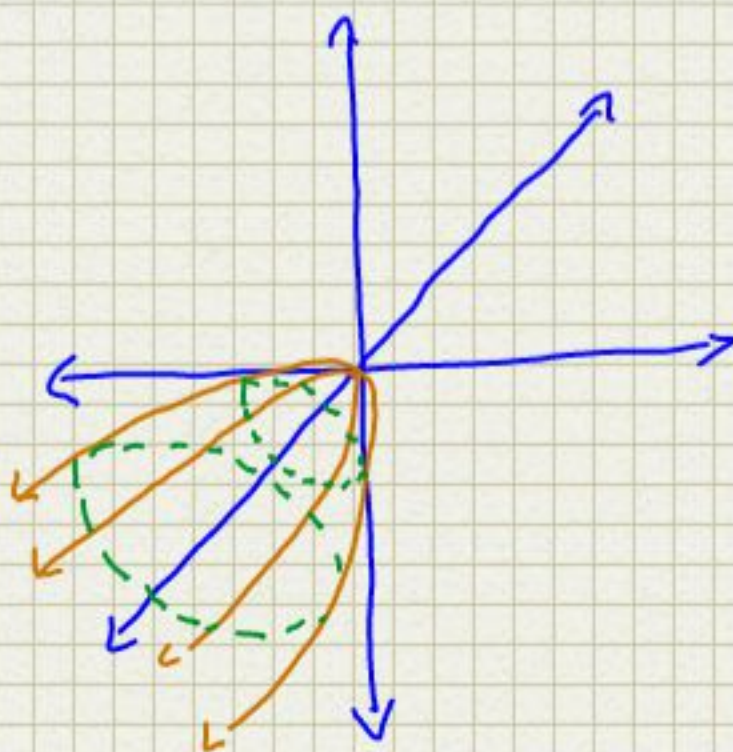
Circular Paraboloid  
 $z = x^2 + y^2$

Elliptic Paraboloid

$$c(z-l) = \frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2}$$

\* c dictates if paraboloid opens up or down

$$z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$$



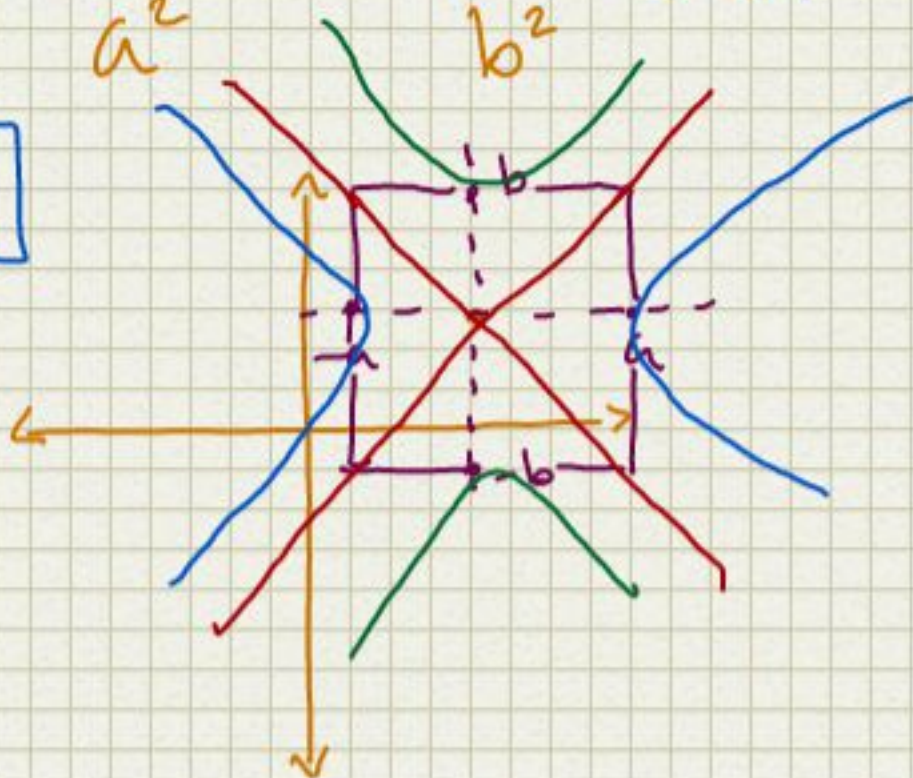
2D

Hyperbola

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = \pm 1$$

+1

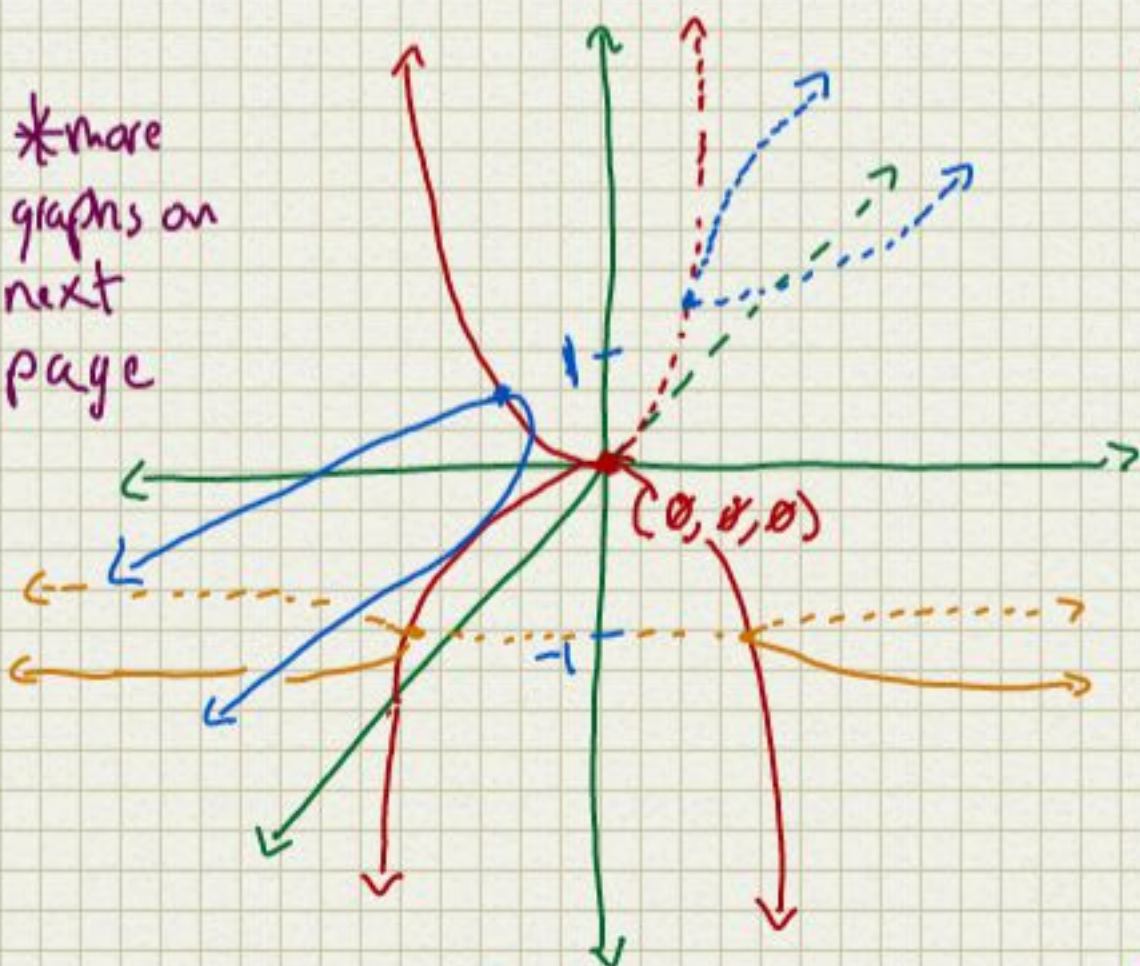
-1



### 3D Hyperbolic Paraboloid

$$c(z-l) = \frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2}$$

\*more  
graphs on  
next  
page



$$\begin{cases} z = -1 \\ -1 = x^2 - y^2 \end{cases}$$

$$z = x^2 - y^2$$

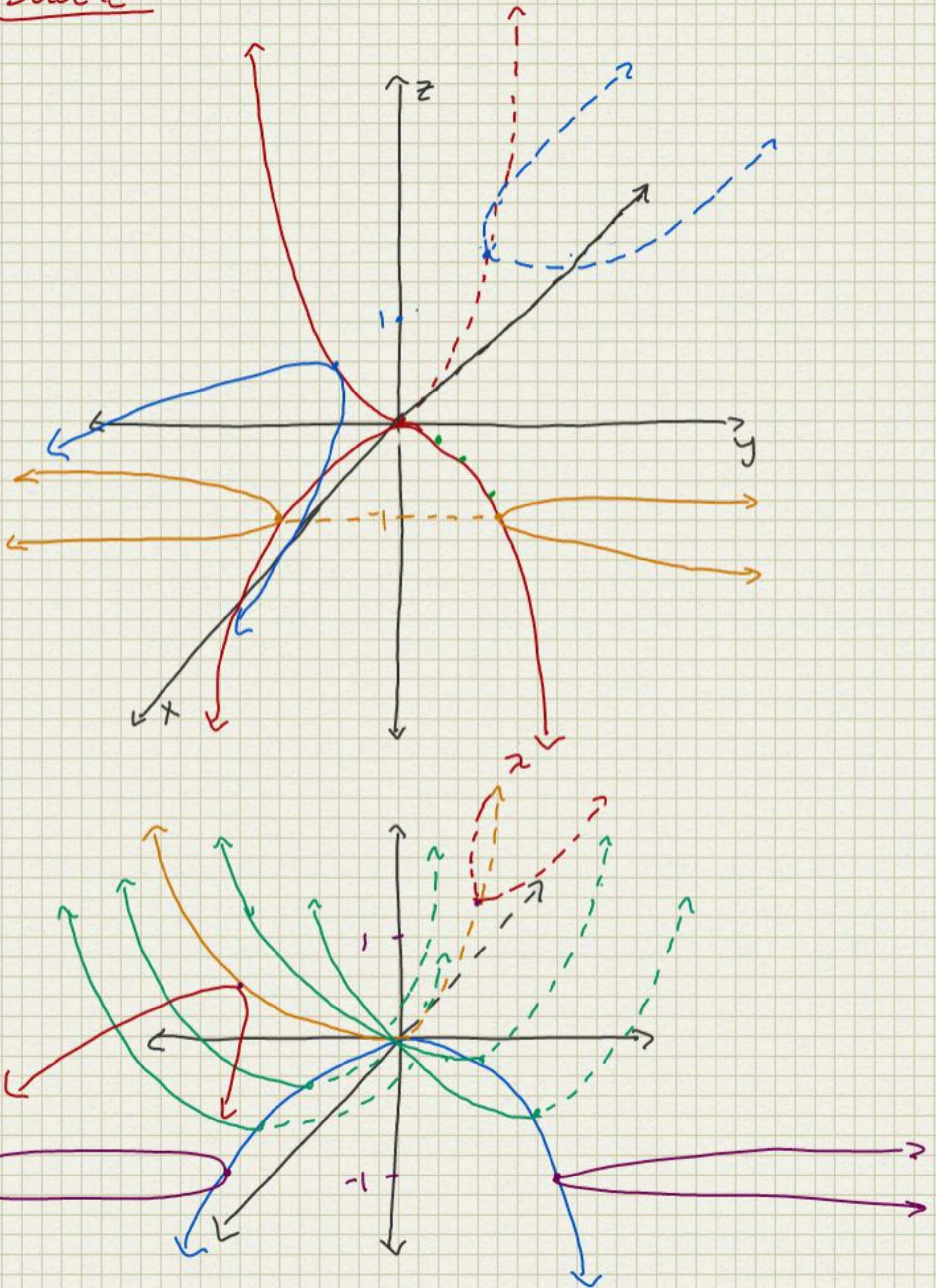
$$\begin{cases} z = 0 \\ 0 = x^2 - y^2 \end{cases}$$

$$\begin{cases} x = 0 \\ z = -y^2 \end{cases} \quad * \text{ on } x\text{-}z \text{ plane}$$

$$\begin{cases} y = 0 \\ z = x^2 \end{cases} \quad * \text{ on } y\text{-}z \text{ plane}$$

$$\begin{cases} z = 1 \\ 1 = x^2 - y^2 \end{cases} \quad * \text{ intersect parabola @ } z = 1$$

Saddle



# Elliptic Hyperboloid

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} - \frac{(z-l)^2}{c^2} = \pm 1$$

**+1**

one sheet

≠ all quadratic terms

two w/ same signs, one opposite

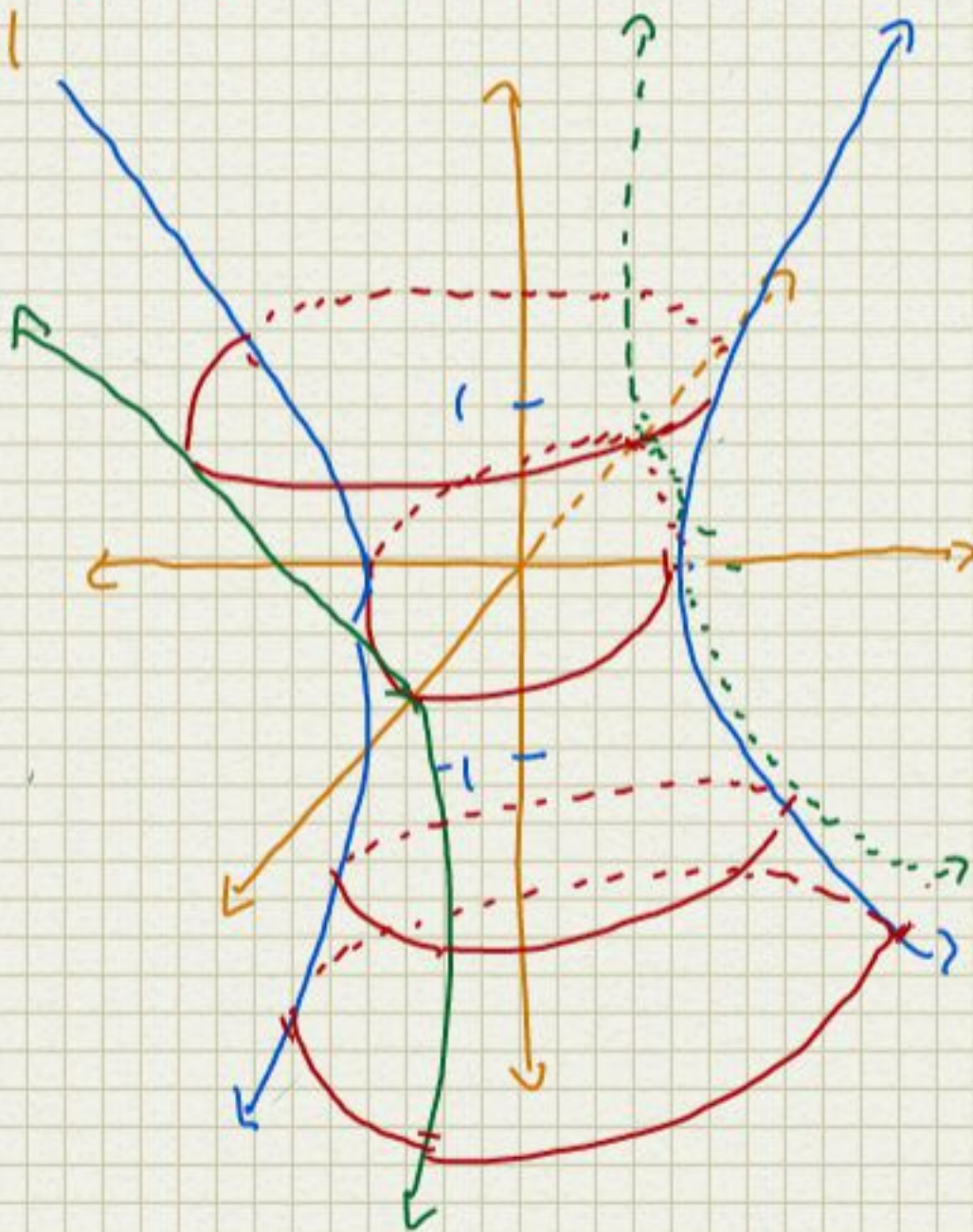
$x^2$  &  $y^2$  agree w/ right hand side

$$x^2 + y^2 - z^2 = 1$$

$$\left. \begin{array}{l} z=0 \\ x^2 + y^2 = 1 \end{array} \right\}$$

$$\left. \begin{array}{l} x=0 \\ y^2 - z^2 = 1 \end{array} \right\}$$

$$\left. \begin{array}{l} y=0 \\ x^2 - z^2 = 1 \end{array} \right\}$$



2 sheets

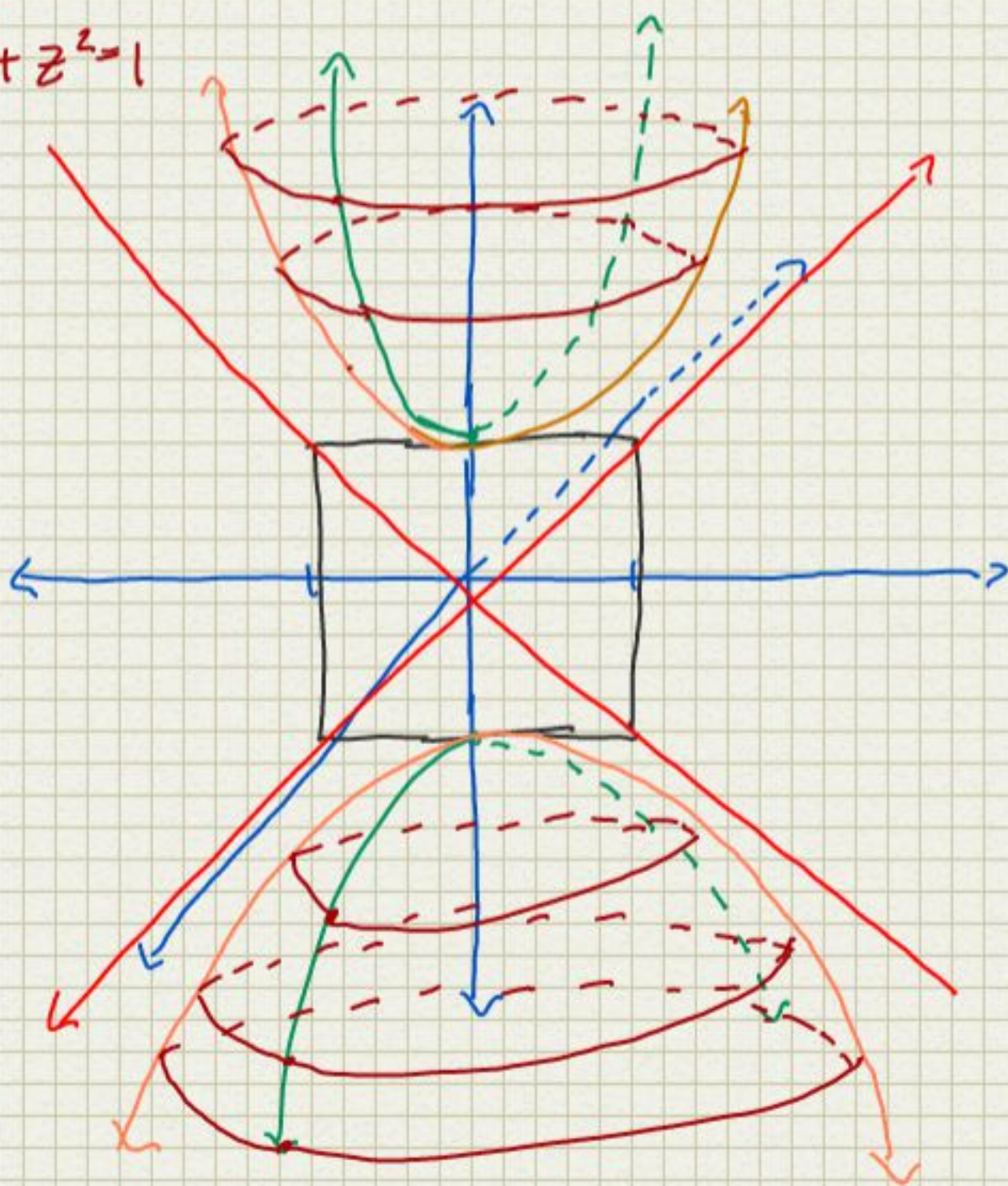
$Z^2$  agrees w/ RHS

$$x^2 + y^2 - z^2 = -1$$

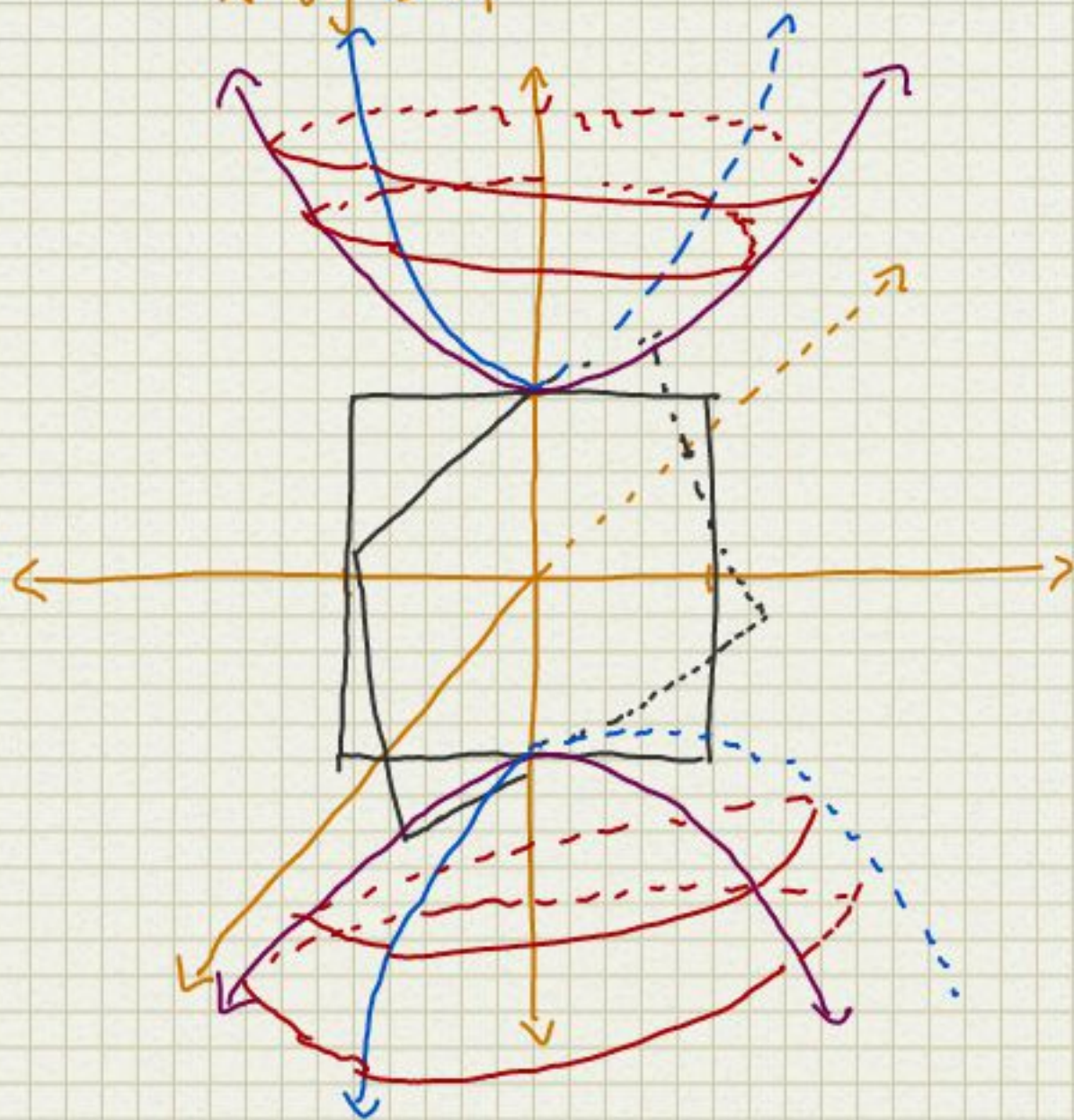
~~$\left\{ \begin{array}{l} z = 0 \\ -x^2 - y^2 = 1 \end{array} \right.$  no solution~~

$\left\{ \begin{array}{l} x = 0 \\ -y^2 + z^2 = 1 \end{array} \right.$  (x-z plane)

$\left\{ \begin{array}{l} y = 0 \\ -x^2 + z^2 = 1 \end{array} \right.$



$$\begin{cases} z = \pm \sqrt{5} \\ -x^2 - y^2 + 5 = 1 \\ x^2 + y^2 = 4 \end{cases}$$



$$-x^2 - y^2 + z^2 = \epsilon$$

(zero)

\* as  $\epsilon$  approaches 0 the squares (asymptotes) shrink and approach the origin.

Cone

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} - \frac{(z-l)^2}{c^2} = 0$$

$$x^2 + y^2 - z^2 = 0$$

$$z = \pm \sqrt{x^2 + y^2}$$

$$z = \sqrt{x^2 + y^2}$$

$$z = -\sqrt{x^2 + y^2}$$

