

Final Exam Formulation  
Math 5320

The final exam will consist of problems of the following types:

1. Problems and/or direct calculations illustrating the operations/arithmetic of  $\mathbb{C}$   
[Similar to problem 1 or 2 on Exam I]
2. Verification of a topological property of a metric space (a set  $A$  is open if condition XXX – a set  $A$  is closed if condition YYY – a point  $x$  is a limit point of a set  $A$  if condition ZZZ – a set  $K$  is compact if condition WWW, etc.)  
[Similar to problem 3, 4, 5 or 6 on Exam I]
3. Classification Problem (which of the following sets are open, closed, bounded, connected, compact, etc.)  
[Similar to problem 8 on Exam I]
4. Find the radius of convergence of a power series  
[Similar to problem 1 on Exam II]
5. Construct a conformal map from one region  $G$  to another  $H$   
[Similar to problem 4 or 6 on Exam II - TakeHome]
6. Determine the image of a specific region under a specific Möbius transformation  
[Similar to problem 5 on Exam II]
7. Use the Cauchy-Riemann equations to:
  1. Verify a function is or is not analytic on a region
  2. Verify a function is constant on a region  
[Similar to problem 2 on Exam II]
  3. Construct a harmonic conjugate of a given harmonic function on a region  
[Similar to problem 7 on Exam II - TakeHome]
8. Verify a (complex) functional identity  
[Similar to problem 3 on Exam II]

9. Evaluate line integrals:
    1. Using Theorem 1.9 for piece-wise smooth paths of integration
    2. Using the Fundamental Theorem of Calculus for Line Integrals
    3. Using Cauchy's Integral Formula #0 (and its corollaries)
    4. Using Cauchy's Theorem #0
  10. Apply Louisville's Theorem
  11. Apply the Identity Theorem
  12. Apply Cauchy's Estimate
  13. Apply the corollaries to Theorem 2.8
  14. State and prove certain theorems
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Problems representing Question Types 1 - 8 will constitute 40% of the exam

Problems representing Question Types 9 - 14 will constitute 60% of the exam