

**SOME USEFUL REDUCTION FORMULAS**  
**MATH 1352**

$$(1) \quad \int \cos^n(x) dx = \frac{1}{n} \cos^{n-1}(x) \sin(x) + \frac{n-1}{n} \int \cos^{n-2}(x) dx$$

$$(2) \quad \int \sin^n(x) dx = -\frac{1}{n} \sin^{n-1}(x) \cos(x) + \frac{n-1}{n} \int \sin^{n-2}(x) dx$$

$$(3) \quad \int \tan^n(x) dx = \frac{1}{n-1} \tan^{n-1}(x) - \int \tan^{n-2}(x) dx$$

$$(4) \quad \int \cot^n(x) dx = -\frac{1}{n-1} \cot^{n-1}(x) - \int \cot^{n-2}(x) dx$$

$$(5) \quad \int \sec^n(x) dx = \frac{1}{n-1} \sec^{n-2}(x) \tan(x) + \frac{n-2}{n-1} \int \sec^{n-2}(x) dx$$

$$(6) \quad \int \csc^n(x) dx = -\frac{1}{n-1} \csc^{n-2}(x) \cot(x) + \frac{n-2}{n-1} \int \csc^{n-2}(x) dx$$

$$(7) \quad \int \sin^p(x) \cos^q(x) dx \\ = \frac{1}{p+q} \sin^{p+1}(x) \cos^{q-1}(x) + \frac{q-1}{p+q} \int \sin^p(x) \cos^{q-2}(x) dx$$

$$(8) \quad = -\frac{1}{p+q} \sin^{p-1}(x) \cos^{q+1}(x) + \frac{p-1}{p+q} \int \sin^{p-2}(x) \cos^q(x) dx$$

$$(9) \quad \int \frac{1}{(a^2 + x^2)^{n+1}} dx = \frac{1}{2na^2} \frac{x}{(x^2 + a^2)^n} + \frac{2n-1}{2na^2} \int \frac{1}{(x^2 + a^2)^n} dx$$